


**ASTR 1040: Stars & Galaxies**



Etched Hourglass Nebula

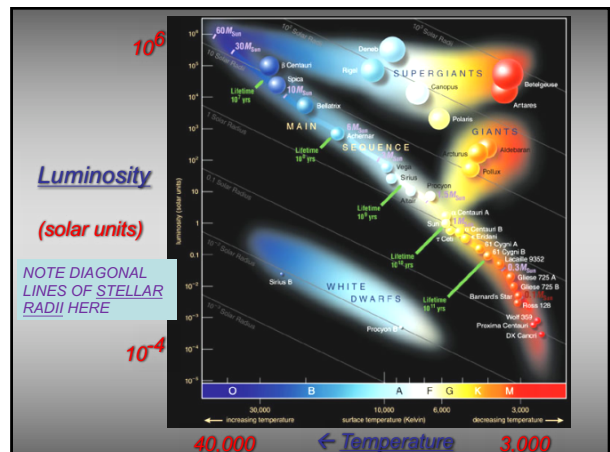
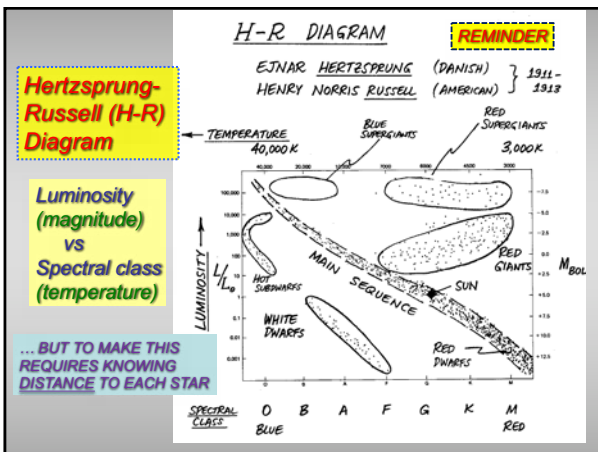
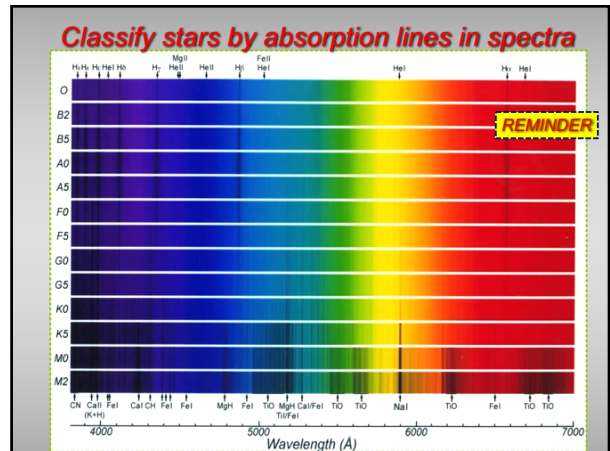
Prof. Juri Toomre TAs: Peri Johnson, Ryan Horton  
Lecture 12 Thur 22 Feb 2018  
zeus.colorado.edu/astr1040-toomre

**Stuff to do**

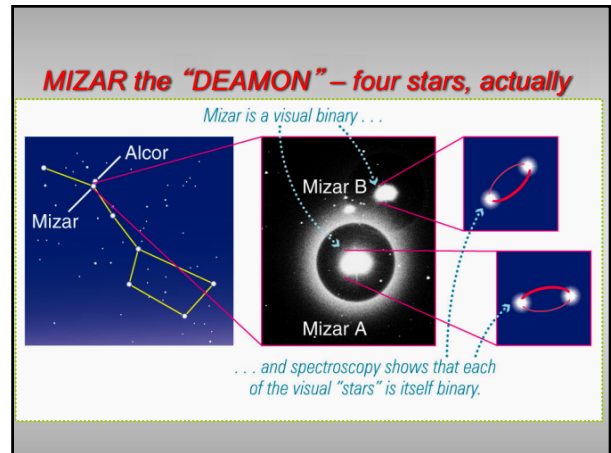
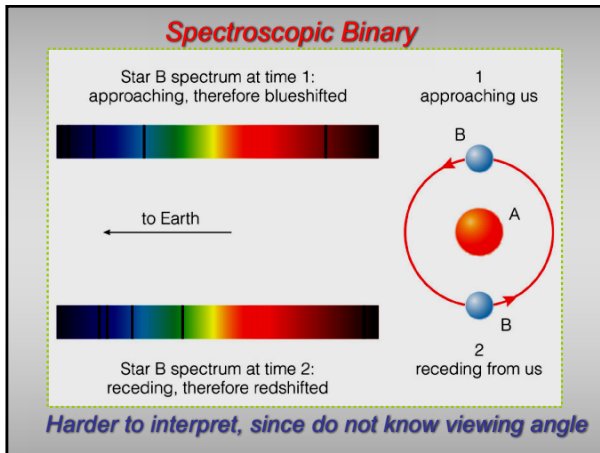
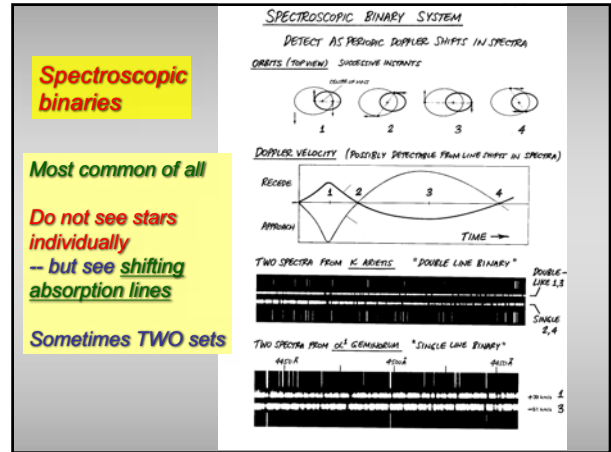
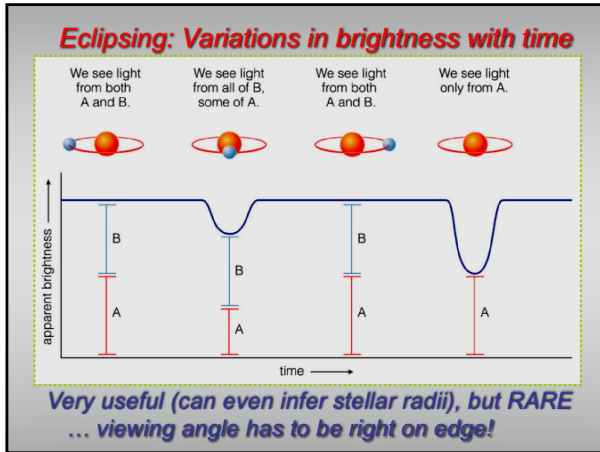
- Paper shuffle:** Homework #5 due, new HW #6 passed out. Graded MT-Exam 1 still available, and so too HW #4 (and earlier), plus answers
- Observatory #3** last night (report)
- Re-read 15.3 Star Clusters with care, and review all of Chap 15 "Surveying the Stars"
- Read 16.1 "Stellar Nurseries" & 16.2 "Stages of Star Birth" for Tues lecture (getting to the Main Sequence)

**Topics for Today**

- Brief review of roadmap to the stars: Hertzsprung-Russell (H-R) diagram
- Binary stars** allow us to measure MASS
- Why O and B stars are so luminous on MS?
- C-N-O cycle** dominates fusion burning of H in massive stars, really pours out the energy
- Explains observed **MASS-LUMINOSITY** relation
- Estimate lifetime on the main sequence (MS)
- What **star clusters** can tell us







**Recall from Chap 3 :**

**KEPLER** devised 3 laws for planetary (or stellar) motions

**In 1687, NEWTON** explained them as balance of gravity and centrifugal force

**GRAVITY (INVERSE SQ LAW), ELLIPTICAL ORBITS AND ANGULAR MOMENTUM** (INVERSE)

- ARISTOTLE, COPERNICUS (1543), TYCHO BRAHE (~160)
- "PLANET OBJECTS" MOVE ON CIRCLES (OR CIRCULAR ORBITES)
- KEPLER (1609, 1618) : LAWS OF PLANETARY MOTION

ELLIPTIC (CIRCLE IS 200% ECCENTRICITY)

1<sup>st</sup> LAW: PLANETS ORBIT SUN ON ELLIPSES, SUN AT ONE FOCUS (COMBINATION)

2<sup>nd</sup> LAW: ALL PLANETS MOVE ABOUT SUN, SWIFTEST BEING NEAREST TO SUN

3<sup>rd</sup> LAW:  $(\text{ORBITAL PERIOD})^2 = (\text{AVERAGE DISTANCE})^3$  [AU]

NEWTON (1687):

GRAVITY FORCE:  $F = G \frac{M_1 M_2}{d^2}$

**DOUBLE STARS: WEIGHING THEM**

BINARIES HELP DETERMINE STELLAR MASS & RADIUS

MEASURE: PERIOD (ONLY)

ORBITAL SPEED (SPECTROSCOPIC BINARIES)

SEPARATION (VISUAL BINARIES)

RECALL KEPLER'S THIRD LAW:

$$(M_1 + M_2) \times P^2 = a^3$$

MASS, SOLAR UNITS (UNKNOWN) PERIOD, YEARS (MEASURED) SEPARATION, A.U. (EARTH-SUN DIST) (MEASURED)

⇒ PERIOD & SEPARATION ⇒ MASS

ECLIPSING BINARIES:

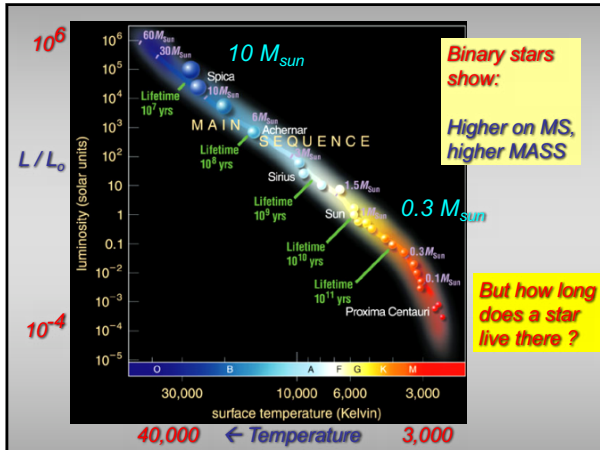
ORBITAL SPEED & ECLIPSE DURATION ⇒ RADIUS (INDEPENDENT MEASURE)

**So why all the fuss with BINARIES?**

**Can really "weigh" a star !**

**STELLAR MASSES** can be inferred from watching orbits

(via law of gravity – Kepler and Newton)



### Brightness / Distance Clicker Q

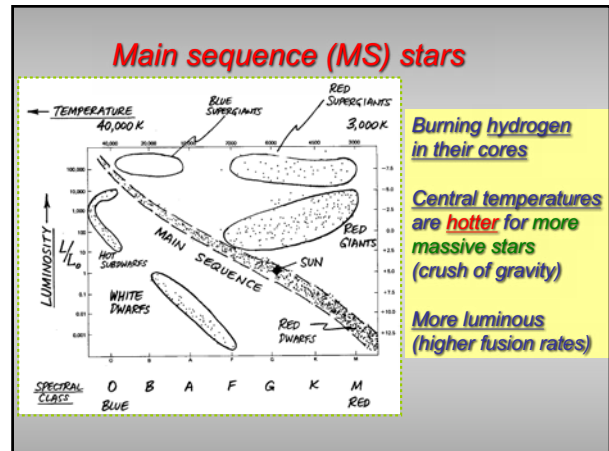
**B.**

- Leonardo and Guinevere are two stars that have the same apparent brightness. Leonardo has a larger parallax angle than Guinevere. Which star is more luminous?

- A. Leonardo
- B. Guinevere
- C. Cannot determine from data given

### Brightness vs Distance

- Leonardo has a larger parallax angle -- thus he is closer to us
- They both have the same APPARENT brightness, but Leo is closer
- B. Guinevere** must be more luminous



### Lifetimes on Main Sequence (MS)

- Stars spend 90% of their lives on MS
- Lifetime on MS = amount of time star burns hydrogen (gradually) in its core
- For Sun, this is about 10 billion years
- For more massive stars (OBAF), lifetime is (much) shorter
- For less massive stars (KM), lifetime is longer
- But how do we get these numbers?

### Look at broad sample, to figure out any lifespan

- Stars take millions to billions of years to go through their life stages - we rarely see a single star change
- Observing many different stars lets us figure out the sequence of a single star's life

**P-P Chain & C-N-O Cycle**

Both fusion processes occur in parallel, but C-N-O makes far more energy at higher temperatures

Stars hotter than F1, C-N-O wins

**THERMONUCLEAR FUSION: HYDROGEN BURNING**

**PROTON-PROTON CHAIN**

**C-N-O CYCLE**

C-N-O CYCLE DOMINATES ENERGY PRODUCTION AT HIGHER TEMPERATURES:

$$\begin{aligned}
 &^{12}\text{C}_6 + ^1\text{H}_1 \rightarrow ^{13}\text{N}_7 + \gamma \\
 &^{13}\text{N}_7 \rightarrow ^{13}\text{C}_6 + e^+ + \nu \\
 &^{13}\text{C}_6 + ^1\text{H}_1 \rightarrow ^{14}\text{N}_7 + \gamma \\
 &^{14}\text{N}_7 + ^1\text{H}_1 \rightarrow ^{15}\text{O}_8 + \gamma \\
 &^{15}\text{O}_8 \rightarrow ^{15}\text{N}_7 + e^+ + \nu \\
 &^{15}\text{N}_7 + ^1\text{H}_1 \rightarrow ^{12}\text{C}_6 + ^4\text{He}_2
 \end{aligned}$$

4 HYDROGEN + CARBON → HELIUM + ENERGY + CARBON TO RECYCLE!

**C-N-O Fusion Cycle**

Key: electron, neutrino, positron, gamma ray, neutron, proton

Can provide vast luminosity for massive stars on MS

**C-N-O Cycle (another view)**

Key: neutron, proton, positron, neutrino, gamma ray

**Main Sequence:**

range of stellar properties

L range is biggest!

**THE MAIN SEQUENCE:**

STARS BURNING HYDROGEN IN CORE

RANGE OF PROPERTIES

(RED GIANTS, WHITE DWARFS NOT MAIN SEQUENCE STARS: SHOW DIFFERENT EXTREMES OF R, L, ...)

SUN IS "INTERMEDIATE" MAIN SEQ. STAR

MASS: 0.01 → 100 M<sub>⊙</sub>

TEMPERATURE: ~ 2,000 → 100,000 K (SURFACE)

RADIUS: 0.01 → 100 R<sub>⊙</sub>

LUMINOSITY: 0.001 → 100,000 L<sub>⊙</sub>

LUMINOSITY ~ (MASS)<sup>3.8</sup>

RADIUS ~ (MASS)<sup>0.75</sup> (ROUGHLY)

**"Observed" MASS - LUMINOSITY relation for main sequence**

But why such a steep variation with mass?

BIGGER CRUSH OF GRAVITY needs...

→ HIGHER central PRESSURE (or temperature)

→ FASTER BURNING (CNO-fusion-cycle comes into play)

**MASS-LUMINOSITY RELATION MAIN SEQUENCE STARS**

LUMINOSITY ~ MASS<sup>3.8</sup>

L ~ M<sup>3.8</sup> OR NEARLY, ~ M<sup>4</sup>

**L ~ M<sup>4</sup>**

MASSSES DETERMINED MOSTLY FROM BINARY PAIRS

⇒ MAIN SEQUENCE IS REALLY A SEQUENCE IN STELLAR MASS (NOT EVOLUTION!)

**How long can stars burn H in their cores?**

**TIME TO BURN UP HYDROGEN IN CORE ... OR "LIFE ON MAIN SEQUENCE"**

OTHER STARS COMPARED TO SUN:

ENERGY E<sub>TOTAL</sub> ∝ MASS (∝ M)

LUMINOSITY L ∝ (MASS)<sup>3.8</sup> (∝ M<sup>4</sup>) ← MASS-LUMINOSITY RELATION

LIFETIME t<sub>LIFE</sub> ~ E<sub>TOTAL</sub> / L ∝ M<sup>-3</sup> (ROUGHLY)

⇒ MASSIVE STARS HAVE SHORT LIVES!

MASS (M <sub>⊙</sub> )	LIFETIME (MILLION YEARS)
1	10,000 MY ≈ 100BY
2	700
3	250
5	70
10	20
15	10
30	5 (LEVEL OFF AT A FEW MY)

More massive star have (very) short lives