

## ASTR 1040: Stars & Galaxies



Whirlpool  
Galaxy M51

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Lecture 11 Tues 20 Feb 2018  
[zeus.colorado.edu/astr1040-toomre](http://zeus.colorado.edu/astr1040-toomre)

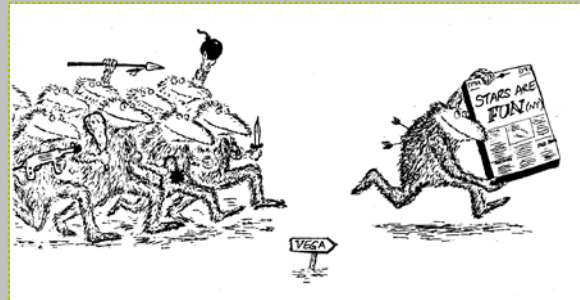
## Logistics

- Read **Chap 15.1: Properties of Stars** with care, then **15.2: Patterns among Stars**
- **Mid-Term Exam 1** returned, with answers, plus cribsheets
- **Homework #4** also returned graded
- **Observatory #3** this Wed 21 Feb, by signup – we try again! (Mixed forecast)

## Topics for Today

- How to **classify other stars**?
- Vital work by **Annie Jump Cannon** in devising a sensible “spectral sequence” for stars
- Why **temperature and spectral lines** are **closely linked** in classifying stars **O B A...M**
- **Cecilia Payne-Gaposhkin** and the “Saha” equation to predict **spectral line strengths**
- Roadmap to the stars: **Hertzsprung-Russell (H-R) diagram**

## So did we really love this exam?



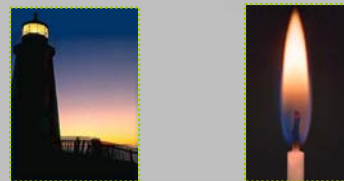
RESULTS FROM FIRST MID-TERM EXAM

## FIRST MID-TERM EXAM

- **Grade boundaries**, based on 110 points (graded on a “curve”):
  - If 99/110 (90%) **or over**, **A’s** [44%]
  - 87/110 (79%) **or over**, **B’s** [46%]
  - 82/110 (75%) **or over**, **C’s** [6%]
- Also +, plain, and – within these ranges

Go through answer sheet – and talk to us if do not understand our choices. Keep exam + answers for future review (comp final)

## Most Basic Problem in Astronomy



Star of given **APPARENT BRIGHTNESS** could be either

- very luminous star far away
- low luminosity star closer by

**Need to know the DISTANCE to the star**

### Inverse Square Law of Brightness

**Apparent Brightness**  
 $\approx \frac{L_0}{(\text{distance})^2}$

### Stellar Luminosity

- What we **measure**: **APPARENT BRIGHTNESS**  
 or how bright it appears to us here on Earth
- What we **want to know**: (absolute) **LUMINOSITY**  
 or how much energy is emitted (joules/sec or watts)
- Need to know **DISTANCE** to the star

### Parallax – to determine distance

- o Measure the **apparent movement of stars** over a year
- o Movement is caused by **Earth's movement around the Sun**
- o Closer objects will move more than farther objects

### How Stellar Parallax Works

### Class self-demo of parallax

- Your **nose** is the Sun
- Your **left eye** is the Earth in January
- Your **right eye** is the Earth in June

Watch the **apparent motion of your thumb** against a distant reference point (repeat at arm's length)

Which **"move" more** -- closer or farther objects?

### Stellar Parallax: measuring nearby distances

**TRIGONOMETRIC PARALLAX:**  
 GIVES DISTANCE TO NEAR STARS DIRECTLY

BY OBSERVING TARGET STAR FROM DIFFERENT VANTAGE POINTS IN EARTH'S ORBIT → STAR APPEARS TO MOVE IN LOOP IN SKY OVER 1 YEAR (COMPARE TO DISTANT STARS)  
 1/2 ANGLE OF LOOP = PARALLAX ANGLE P

DISTANCE TO STAR  $d = \frac{1}{P}$

IF P = 1 ARCSEC (1"), DISTANCE IS 1 PARSEC (PC) (PARALLAX SECOND)

PC = 3.26 LY = 206,265 A.U.


LIMITED BY ACCURACY OF STAR POSITIONS

FROM EARTH: 0.01" — 100 PC  
 SPACE TELESCOPE: 0.001" — 1000 PC (~1 kpc)

LIMITING FACTOR IS BLURRING, FURTHER DUE TO TURBULENCE OF EARTH'S ATMOSPHERE

**Best parallax measurers:**  
**Hipparcos satellite 1989-1993**  
**GAIA satellite Dec 2013 →**

- Space measurements not affected by atmosphere
- Measurement made many times until accurate to  $-0.001$  arcsec (Hipparcos  $\rightarrow 1,600$  light years)
- 100,000 stars mapped; 2.5 million lesser accuracy
- **GAIA:** 10 micro-arcsec, billion stars; 10,000+ ly



**Clicker recall: What is net inward force on evacuated "oil barrel"?**

- A: 200 lbs
- B: 500 lbs
- C: 2,000 lbs
- D: 5,000 lbs
- E: 50,000 lbs

**REMINDER**

**Measuring Surface TEMPERATURE**

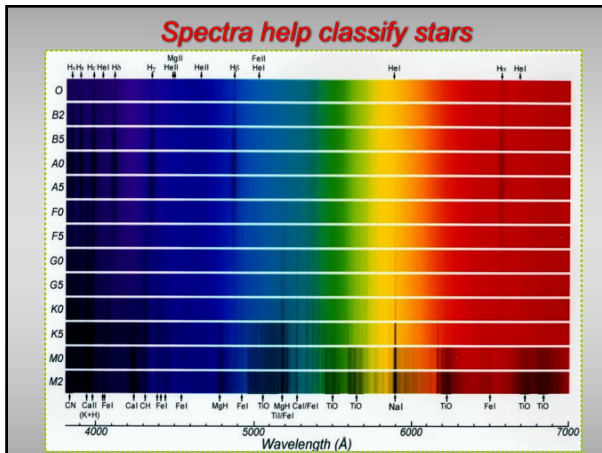
Shape of spectrum good ... but **spectral lines** much better

**ANALYZING STARLIGHT**

MEASURED SPECTRUM  
 INTENSITY vs WAVELENGTH  
 EMISION LINES (BLACK)  
 ABSORPTION LINES (DARK)  
 CONTINUUM

SHAPE OF CONTINUOUS SPECTRUM GIVES ESTIMATE OF STAR'S SURFACE TEMPERATURE  
 BUT .... ABSORPTION LINES (AND THEIR STRENGTHS) ARE EVEN MORE SENSITIVE MEASURE OF TEMPERATURE (AND ALSO OF COMPOSITION)  
 ... PRESENCE OF EMISSION LINES ALSO HELPFUL

TYPICAL STELLAR SPECTRUM  
 SLOW-TYPE STAR  
 BLUE vs RED vs 4000 Å vs 6000 Å vs WAVELENGTH




**A bit of history: Classifying Stars**

World War I, Harvard College observatory


Women were hired by Pickering as "calculators" to help with a new survey of the Milky Way

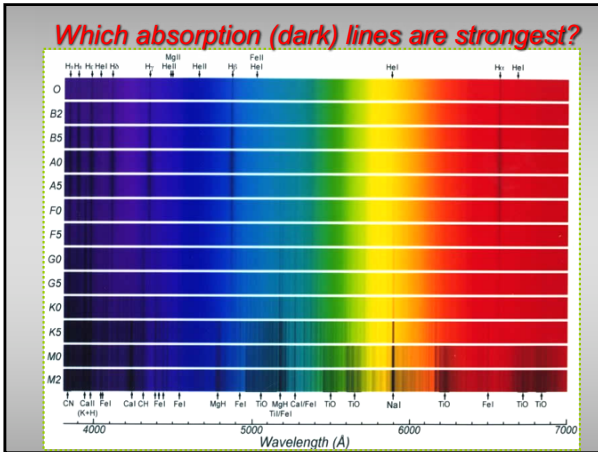
Most had studied astronomy, but were not allowed to work as scientists



**Devising the strange temperature code**

- **Original classification of spectra (1890) was:**  
**A = strongest hydrogen feature**  
**B = less strong hydrogen ...C, D, etc.**
- **Annie Jump Cannon realized that a different sequence made more sense (~1910)**  
**→ OBAFGKM !!**





**Spectral Classification: O B A F G K M**

Which **ABSORPTION** lines are strongest

**Hottest stars: O B**  
ionized helium only

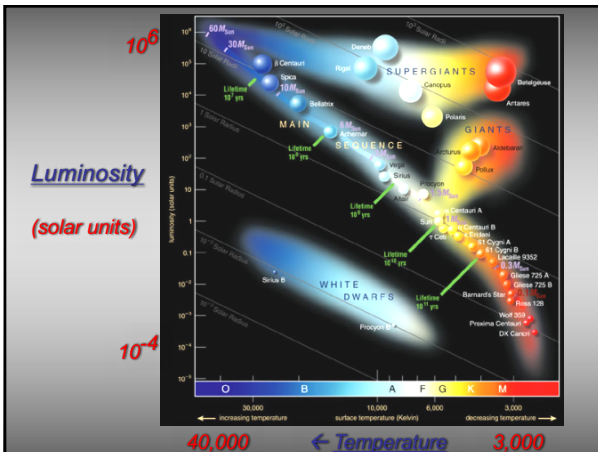
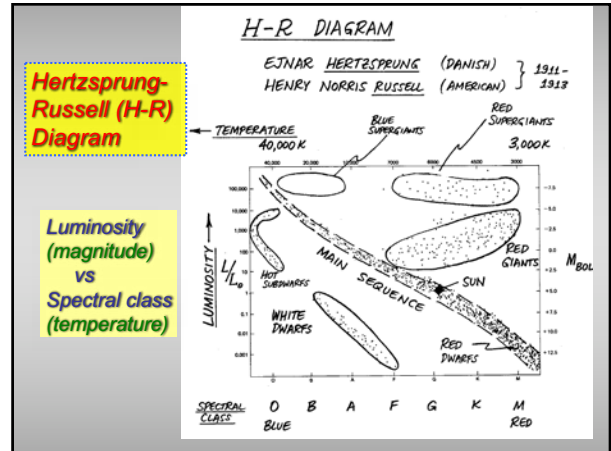
**Hot stars: A F** helium, hydrogen

**Cooler stars: G**  
hydrogen, heavier atoms

**Cooltest stars: M**  
molecules, (complex absorption bands)

**H - R Namesakes**

**Ejnar Hertzsprung**      **Henry Norris Russell**



Cecelia figured out **WHY** stellar spectra are so different: **TEMPERATURE**

- She showed that **SURFACE TEMPERATURE** is the big factor (not composition)
- She used the newly-devised **SAHA EQUATION**, estimating how many electrons remain attached to atoms as temperature is changed (or the level of ionization)

**Cecelia Payne-Gaposchkin**  
(Harvard PhD thesis 1925)

**O B A F G K M** → decreasing temperature

**Why temperature and spectral lines are linked?**

**SAHA gives the answer:**

can estimate "population of different energy levels" in H, He ...

and **ionization** (continuous crash, bang, relax, do it again)

**STUDY OF STELLAR ATMOSPHERES: WHY ARE SPECTRAL LINES AND TEMPERATURE RELATED?**

RECALL TEMPERATURE OF GAS IS MEASURE OF AVERAGE KINETIC ENERGY (OR VELOCITY<sup>2</sup>) OF ATOMS

AND... THE FASTER ATOMS COLLIDE, THE MORE THEY DISTURB OR DISTURBE ELECTRONS

SAHA EQUATION (MUCH HAD SAHA, 1924, INDIAN PHYSICIST)

PREDICTS RELATIVE NUMBER OF ATOMS IN EACH EXCITED STATE OF ELECTRON (ENERGY LEVEL), GIVEN TEMPERATURE & PRESSURE OF GAS

→ SPECTRAL LINE STRENGTHS (AND VICE VERSA)

JUST WHICH PHOTONS CAN BE ABSORBED DEPENDS ON WHICH ELECTRON ORBITS ARE POPULATED!

FOR HYDROGEN, VISIBLE (BALMER) SERIES OF STRONG ABSORPTION LINES IF MANY ATOMS IN EXCITED  $n=2$  STATE

→ TEMP  $\sim 10,000$  K

**SAHA predicts spectral line strengths with temperature**

**WHAT SAHA PREDICTS:**

SPECTRAL CLASS

SPECTRAL LINE STRENGTH

TEMPERATURE (K)

SAHA EQUATION FOR HYDROGEN:

- FOR H $\alpha$  LINE (H $\alpha$ ), FLUX INCREASES AS TEMPERATURE INCREASES
- FOR H $\beta$  LINE (H $\beta$ ), FLUX INCREASES AS TEMPERATURE INCREASES
- FOR H $\gamma$  LINE (H $\gamma$ ), FLUX INCREASES AS TEMPERATURE INCREASES
- FOR H $\delta$  LINE (H $\delta$ ), FLUX INCREASES AS TEMPERATURE INCREASES
- FOR H $\epsilon$  LINE (H $\epsilon$ ), FLUX INCREASES AS TEMPERATURE INCREASES

**Puzzle Clicker: Stellar Parallax**

- The biggest ground-based telescopes with adaptive optics can measure stars positions with accuracies of about **0.05 arcsec**. How far away could they map the positions of stars via parallax?

**A.** 2 pc = 6.5 light years

**B.** 20 pc = 65 light years

**C.** 200 pc = 650 light years

**B.**

**Parallax**

- B. maximum distance** is set by the **accuracy** with which you can measure positions in the sky (space does better than ground)

Distance (pc) =  $1 / 0.05 \text{ arcsec} = 20 \text{ pc} = 65 \text{ ly}$

$d \text{ (in parsecs)} = 1 / p \text{ (in arcsec)}$

**Further refinements:**

**DECIMAL SUBDIVISION**

**LUMINOSITY CLASSES** how narrow are absorption lines

**Sun is: G2 V COLOR CLASS**

**STARS: REFINEMENTS IN CLASSIFYING THEM**

SUBDIVISIONS OF SPECTRAL COLOR CLASSES:

A G0 G1 G2 G3 G4 G5 G6 G7 G8 G9

LUMINOSITY CLASSES:

FOR THE SAME COLOR OF STAR (SPECTRAL CLASS), LARGER STARS HAVE NARROWER ABSORPTION LINES

WHY? PRESSURE AT SURFACE ARE LESS, ATOMS ARE LESS DISTURBED BY COLLISIONS

EXAMPLES:

AS I AS II AS III AS IV AS V

Hydrogen Balmer lines: G G Y R

Wavelengths: 6500 6000 5500 5000

THIS LUMINOSITY (OR "BRIGHTNESS") CLASSES

I SUBGIANTS BRIGHT GIANTS

II GIANTS

III SUBGIANTS

IV MAIN SEQUENCE (OR DARK) FAINTLY

BRIGHTNESS

**Magnitudes: Apparent vs Absolute**

- Giving measures to **stellar luminosities**
- Built on choices made by Greeks!

**Stellar MAGNITUDES**

**Weird system: brighter is smaller magnitude, even negative!**

**Of cultural importance, even if a bit confusing (secret society!)**

**MAGNITUDES: BLAME WEIRD SCALE ON GREEKS ... AND REPAIR BY HERSCHEL**

- GREEKS ASSIGNED  
 BRIGHTEST STAR MAGNITUDE 1  
 FAIEST STAR VISIBLE TO EYE MAG 6 } DIFFERENCE OF 5
- HERSCHEL CONCLUDED THIS WAS ABOUT 100:1 IN BRIGHTNESS  
 ASSIGNED APPARENT MAGNITUDE  $m_p = 0$  TO BRIGHTEST STAR VEGA AND RICHL KEAT
- NOW THE PRESENT SYSTEM:  
 BRIGHTNESS UP  $\uparrow$  BY FACTOR 2.512  
 MAGNITUDE DOWN  $\downarrow$  BY 1 UNIT

MAGNITUDE	RELATIVE BRIGHTNESS
5	1.0
4	2.512
3	6.310 = $(2.512)^2$
2	15.849 = $(- )^3$
1	39.811 = $(- )^4$
0	100.000 = $(- )^5$

**Measuring BRIGHTNESS magnitudes**

**m** apparent mag: what looks like in sky

**M** absolute mag: what would look like if at 10pc distance (LUMINOSITY)

**MEASURES OF BRIGHTNESS FIRST STARS, NOW GALAXIES...**

- APPARENT MAGNITUDE  $m$**   
 ACTUALLY MEASURE HOW BRIGHT AN OBJECT APPEARS IN SKY  
 DEPENDS ON SPECTRAL REGION (COLOR) WHERE MEASURED  
 USE FILTERS:  
 U UBVRI  
 B BLUE  $m_B$   
 V VISUAL  $m_V$   
 ETC...

- BOLOMETRIC MAGNITUDE**  
 ADD UP BRIGHTNESS AT ALL WAVELENGTHS ... BUT DIFFICULT TO MEASURE
- ABSOLUTE MAGNITUDE  $M$**   
 MAGNITUDE STAR WOULD HAVE IF AT DISTANCE OF 10 PARSECS (32.6 LY)  
 NEED  $m$  AND DISTANCE!

**(Slightly) screwy world of MAGNITUDES**

**IF can estimate distance, then can determine  $M$  given  $m$**

**$M = m$  if at distance 10pc**

**MAGNITUDES: HANDY RESULTS TO RECALL**

5 MAGNITUDES = FACTOR OF 100 IN BRIGHTNESS

MAGS. CAN BE NEGATIVE

BOL. MAG. < APPARENT MAG.

ABSOLUTE MAGNITUDE  $M <$  APPARENT MAG  $m$  IF DISTANCE  $>$  10 PC  
 $M >$   $m$  IF DISTANCE  $<$  10 PC

VISUAL MAGNITUDES OF "NEARBY OBJECTS"

Object	Apparent Magnitude ( $m_v$ )	Distance (ly)	Absolute Magnitude ( $M_v$ )
Sun	-26.7	$1.5 \times 10^{-8}$	-4.8
Moon (Full)	-12.5	$4.0 \times 10^5$	+32.1
Venus (at brightest)	-4.4	$4.4 \times 10^7$	+39.9
Sirius	-1.5	8.6	+1.4
Polaris (Alpha Centauri)	0.0	4.3	+4.4
"Hipp"	0.0	25.0	+5.0
Canopus (Alpha Cygni)	-1.3	$1.6 \times 10^4$	-7.2
601-15 (Dwarf star)	+14.8	11.9	+17.0
Andromeda Galaxy	+3.5	$2.25 \times 10^6$	-21.0

**Clicker: Stellar puzzle B.**

- Two stars, **Antony** and **Cleopatra**, are both of spectral class **M3**, and of the same apparent brightness (magnitude) in the sky. Cleopatra shows narrow absorption lines in her spectrum, Antony broad ones. Which star must be far more distant?
- A. Antony
- B. Cleopatra

**Estimating the size of a star - its RADIUS**

**Stefan-Boltzmann**

**MEASUREMENTS OF STARS:**

TEMPERATURE (FROM SPECTRAL LINES)  
 BRIGHTNESS  
 DISTANCE }  $\Rightarrow$  LUMINOSITY

RECALL STEFAN-BOLTZMANN LAW:

$$L = 4\pi R^2 \times \sigma \times T^4$$

LUMINOSITY (MEASURED) = STAR'S RADIUS (UNKNOWN)  $\times$  CONSTANT  $\times$  TEMPERATURE (MEASURED)

$\Rightarrow$  LUMINOSITY & TEMP  $\Rightarrow$  RADIUS

BUT HOW TO GET THE MASS?  
 (TRICKIER: USE BINARIES)

